

**Micromechanical modelling of elasto-viscoplastic behavior of
near beta-Ti alloys:
Effect of elastic anisotropy on elastic-viscoplastic transition,
incompatibility stresses and slip activity**

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Abstract

The last few years, near beta-titanium alloys benefit from a growing interest and are now competing with quasi-alpha or alpha-beta titanium alloys for airframe forging applications like landing gears and rotor systems. High strength are achieved thanks to the building up of complex microstructures. They are mainly composed of bimodal alpha constituents embedded in a retained beta matrix (with often up to 40% beta phase) [1].

The beta phase is reported to exhibit a highly anisotropic elastic behavior. The published elastic constants are however surprisingly spread with anisotropy coefficients ranging from 1 to 8 [2–5]. Moreover, the influence of the beta-phase elastic anisotropy on the mechanical response of near beta-titanium alloys with complex alpha/beta microstructure is not well understood.

Thus the present work applies an advanced micromechanical model to capture elastic/plastic incompatibilities arising in tensile or fatigue tested near beta-titanium alloys. The mechanical properties are estimated based on a recent elasto-viscoplastic self-consistent model (EVPSC) with “affine” linearization of the viscoplastic flow rule. Its allows a good description of the overall response of heterogeneous materials even when the viscoplastic flow rule is highly nonlinear [6,7].

First we consider a fully beta phase microstructure to account for the influence of the elastic anisotropy, the texture, the morphology of the beta grains on the incompatibility stresses during elastic and viscoplastic responses [8,9].

Then the same micro-mechanical approach is applied to Ti-1023 with alpha-nodular microstructure. Our numerical results show how the elastic anisotropy of both beta and alpha phases affects simultaneously the macroscopic elastic-viscoplastic transition, the microscopic fields, the slip activity for different alpha/beta phase morphologies, volume fractions and crystallographic textures.

Keywords: near beta-titanium alloys, polycrystals, homogenization, elasto-viscoplasticity, elastic anisotropy, incompatibility stresses, slip activity.

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